

College of Excellence, nirf 2023– 4<sup>th</sup> Rank (An Autonomous Institution Affiliated to Bharathiar University) (Accredited with 'A++' Grade by NAAC , An ISO 9001:2015 Certified Institution) Peelamedu, Coimbatore – 641004

#### **DEPARTMENT OF MATHEMATICS (PG)**

#### CHOICE-BASED CREDIT SYSTEM & LEARNING OUTCOME BASED

#### **CURRICULAR FRAMEWORK**

**MASTER OF MATHEMATICS** 

2023-2025 Batch

(III SEMESTER)

#### PROGRAMME EDUCATIONAL OBJECTIVES

# The M. Sc Mathematics curriculum is dedicated to preparing students for productive careers after 3-5 years of graduation.

- 1. Apply their knowledge in modern industry or teaching, or secure acceptance in highquality graduate programs in mathematics.
- 2. Development in their chosen profession and/or progress toward an advanced degree
- 3. The trust and respect of others as effective and ethical team members.
- 4. Graduates will become effective collaborators and innovators, leading or participating in efforts to address social, technical and business challenges.
- 5. Promote the culture of interdisciplinary research among all disciplines and applied mathematics.

#### **PROGRAMME LEARNING OUTCOMES**

On the successful completion of the programme, the following are the expected outcomes

- **PLO1:** Students acquire sound analytical and practical knowledge to formulate and solve challenging problems.
- **PLO2:** Students will be able to read and identify mathematical and computational methods in order to solve comprehensive problems.
- **PLO3:** Students are well prepared to take jobs in schools and colleges as Mathematics teachers and Professors, Software Industries, Research and Development Organizations.
- **PLO4:** Students to purse higher studies in Mathematical and Computing Sciences and to clear Competitive exams like SET/ NET/ TET etc.
- **PLO5:** Students to learn and apply Mathematics in real life situations aiming at service to the society.

#### **PROGRAMME SPECIFIC OUTCOMES**

- **PSO1:** Provide Strong foundation and inculcate ample knowledge on topics in pure and applied mathematics, empowering the students to pursue higher degrees at reputed academic institutions
- **PSO2:** Advanced mathematical topics provide opportunities to research students for communication and discussion.
- PSO3: Demonstrate the highest standard of ethics in research.
- **PSO4:** Provide scope for interaction with international researchers and developing collaborations.
- **PSO5:** Provide knowledge of a wide range of mathematical techniques and application of mathematical methods/tools in other scientific and engineering domains.
- **PSO6:** Nurture problem solving skills, thinking, creativity through assignments, project work.
- **PSO7:** Generate publications in reputed mathematical journals.



#### DEPARTMENT OF MATHEMATICS (PG) CHOICE BASED CREDIT SYSTEM & LEARNING OUTCOME BASED CURRICULAR FRAMEWORK SYLLABUS & SCHEME OF EXAMINATION MASTER OF MATHEMATICS 2023 -2025 BATCH & ONWARDS

Sem	Course Code	Title of the course	Instruction hours/ Week	Contact hours	Tutorial	Duration of Examination	СА	Examination BSE Marks	Total	Credits
-	MTH23CEA	Graph Theory	3+3	41/	4/2	-	100	-	100	5
II/III		Or		43						
	MTH2309	Complex Analysis	6	88	2	3	25	75	100	5
	MTH2310	Topology	6	88	2	3	25	75	100	5
	MTH2311	Basics of Cryptography **	6	88	2	3	25	75	100	5
	MTH2312	Fluid Dynamics	6	88	2	3	25	75	100	5
III	MTH23S1	General Course- Research Methodology	2	30	-	3	-	100	100	2
	MTH23E5	Elective III: Mathematical Modelling /	4	58	2	3	25	75	100	3
	MTH23E0	Tensor Analysis								
	MTH23COM	Comprehensive Examination	-	-	-	-	-	100	100	Grade
I - III	17MONL1	Online Course #	-	-	-	-	-	-	-	1*

\*\* Open Book Examination - CIA

 \* Students completing online course through NPTEL and IIT MUMBAI will get a credit of 1, for others completed status will be given

# Self study

COURSE NUMBER	COURSE NAME	CATEGORY	L	Т	Р	CREDIT
MTH2309	COMPLEX ANALYSIS	THEORY	88	2	-	5

- > To present students the elements and importance of the Complex analysis.
- > To define and recognize the basic properties of the complex numbers.
- To enable the students to the differentiability of complex functions and its related theorems.

#### **Course Learning Outcomes**

On the successful completion of the course, students will be able to

	CLO	Knowledge
CLO	Statement	Level
Number		
CLO1	Understand the fundamental properties of the complex numbers that lead to the development of complex analysis	K2
CLO2	Apply the line integrals, curve integrals, singularities and determine the values of integrals using residues.	K3
CLO3	Analysis about limits and to know how they are used in series and problems	K4
CLO4	Evaluate the functions of complex variable in terms of continuity, differentiability and analyticity. Apply Cauchy-Riemann equations and harmonic functions to solve problems	K5
CLO5	Create a rigorous arguments developing the theory underpinning complex analysis	K5

#### Mapping with Programme Learning Outcomes

PLOs CLOs	PLO1	PLO2	PLO3	PLO4	PLO5
CLO1	S	S	S	М	S
CLO2	S	S	S	S	S
CLO3	S	S	М	S	М
CLO4	S	М	S	S	М
CLO5	S	S	М	S	S

S- Strong; M-Medium; L-Low

#### CORE IX - SEMESTER III - COMPLEX ANALYSIS (MTH2309)

Introduction to the concept of analytic function: Limits and continuity - Analytic

functions- Polynomials - Rational functions - Conformality: Arcs and closed Curves - Analytic functions in regions - Conformal Mapping - Length and Area - Linear Transformations: The Linear group - The Cross-ratio - Elementary Riemann Surfaces.

Unit II

Unit I

Complex integration: Line integrals **Rectifiable Arcs** - Line Integrals as Functions of Arcs- **Cauchy's theorem for a rectangle** - Cauchy's theorem in a disk - Cauchy's integral formula: The index of a point with respect to a closed curve - The integer formula - Higher derivatives - **Removable singularities** - Taylor's Theorem - **Zeros and Poles** - The local mapping - The Maximum Principle - chains and cycles.

#### Unit III

The Calculus of Residues: The Residue theorem - The Argument principle - Evaluation of definite integrals - Harmonic functions: The Definitions and basic Properties - **Mean value property** - Poisson's Formula.

Unit IV

Series and Product Developments: Weierstrass theorem - The Taylor Series - The Laurent Series - Partial fractions and Factorization: Partial Fractions - Infinite Products - Canonical Products.

#### Unit V

**The Riemann Mapping Theorem** - Statement and Proof- Boundary Behavior - Use of the reflection principle - Analytic arcs - **Conformal mapping of Polygons**: The Behavior at an angle - **the Schwartz - Christoffel Formula** - Mapping on a rectangle.

#### (18 Hrs)

#### (18 Hrs)

#### (17 Hrs)

(18 Hrs)

# (17 Hrs)

#### TextBook

S. No	Author	Title of the book	Year & Edition	
1.	L.V. Ahlfors	Complex Analysis	2013, III	
	Unit I : Chapter - Chapter - Unit II : Chapter Unit III: Chapter Unit IV: Chapter Unit V : Chapte	<ul> <li>2 Sections 1.1-1.4</li> <li>3 Sections 2.1-2.4- 3.1-3.2 an</li> <li>4 Sections 1.1-1.5, 2.1-2.3, 3</li> <li>r - 4 Sections 5.1-5.3,6.1-6.3</li> <li>r - 5 Sections 1.1-1.3,2.1-2.3</li> <li>er - 6 Sections 1.1-1.4,2.1-2.3</li> </ul>	d 3.4 .1-3.4 and 4.1	

## **Reference Books**

S. No	Author	Title of the book	Publishers	Year &
				Edition
1.	S. Ponnusamy	Foundations of Complex Analysis	Narosa Publisher	2003, II
2.	A.R.Vasistha and Etal	Complex Analysis	Krishna prakashan media pvt ltd	2008, I
3.	A.F.Beardon	Complex Analysis	John Wiley and Sons	1979, I

#### **Course Designer**

- 1. Mrs. K. Sharmilaa, Assistat Professor
- 2.Mrs. R. Sakthikala, Assistant Professor

#### **Course content and Lecture schedule**

			MT			
Module No.	Торіс	No.of hours	CLO's	Content Delivery Method	Student Engagement	Participatory Learning / Experiential Learning / Problem based Learning
		1		UNIT I		
1.	Introduction to the concept of analytic function: Limits and continuity	1	CLO2, CLO4	Lecture – Chalk and Talk / Group reading	Word cloud/ Mind map / Think Write and Share	Participatory Learning
2.	Analytic functions	1	CLO2 CLO3	Lecture, Chalk and Talk, Video Lecture, PPT <u>https://www.yo</u> <u>utube.com/watch?v</u> <u>=P51wtDp7GjA</u>	Post it parade	Experiential Learning
3.	Polynomials	2	CLO2, CLO3, CLO4	Lecture , Chalk and talk/ Picture	Diagrams, Sketchboard	Participatory Learning
4.	Rational functions	2	CLO2,C LO4	Lecture, Chalk and Talk	Quizalize Diagrams, Sketchboard	Experiential Learning
5.	Conformality: Arcs and closed Curves	1	CLO2,C LO4	Video Lecture Chalk and Talk <u>https://www.youtu</u> <u>be.com/watch?v=R</u> T3Yh_jxjYo	Presentation, Group reading and discussion.	Problem-based Learning
6.	Analytic functions in regions	2	CLO1,C LO2, CLO4	Video Lecture , OER <u>https://www.youtu</u> <u>be.com/watch?v=R</u> <u>T3Yh_jxjYo</u>	Quescussion, Pro-con grid	Problem-based Learning
7.	Conformal Mapping	2	CLO2,C LO3, CLO5	Video Lecture Demonstration <u>https://www.youtu</u> <u>be.com/watch?v=R</u> <u>T3Yh_jxjYo</u>	Presentation	Problem-based Learning
8.	Length and Area	1	CLO3,C LO4	Lecture, Quiz	Diagrams, Sketchboard	Experiential Learning
9.	Linear TransformationThe Linear group	2	CLO2,C LO4, CLO5	Lecture , Chalk and talk/ Picture	Diagrams, Sketchboard	Participatory Learning

10.	The Cross-ratio	2	CLO2,C LO3	Demonstration	Presentation	Problem-based Learning
11.	Elementary Riemann Surfaces.	1	CLO3,C LO4	Lecture PPT	Peer teaching	Participatory Learning
				UNIT - II	[	
12.	Complex integration: Line integrals	1	CLO1, CLO2, CLO3	Lecture, PPT	Group discussion	Experiential Learning
13.	Rectifiable Arcs	1	CLO1, CLO2, CLO3	Video Lecture , PPT <u>https://www.youtu</u> <u>be.com/watch?v=X</u> <u>cDIjRet5hw</u>	Think write and share	Experiential Learning
14.	Line Integrals as Functions of Arcs	2	CLO1, CLO2, CLO3, CLO4,	Demonstration	Presentation	Problem-based Learning
15.	Cauchy's theorem for a rectangle	2	CLO2, CLO3, CLO4,	Video Lecture, Group Discussion <u>https://www.youtu</u> <u>be.com/watch?v=A</u> <u>ruIhF83CIY</u>	Diagrams, Sketchboard	Participatory Learning
16.	Cauchy's theorem in a disk	2	CLO2, CLO3, CLO4,	Lecture / OER Seminar	Flipped classroom, Presentation	Participatory Learning
17.	Cauchy's integral formula: The index of a point with respect to a closed curve	2	CLO2, CLO3, CLO4,	Lecture / OER Seminar	Flipped classroom, Presentation	Participatory Learning
18.	The integer formula - Higher derivatives	1	CLO2, CLO3, CLO4,	Lecture, PPT	Group discussion	Experiential Learning
19.	Removable singularities	1	CLO2, CLO3	Video Lecture, Lecture <u>https://www.youtu</u> <u>be.com/watch?v=r</u> <u>bE6EuQLZbY</u>	Presentation, Group reading and discussion.	Problem-based Learning

20.	Taylor's Theorem	1	CLO2, CLO3, CLO4, CLO5	Lecture, PPT	Group discussion	Experiential Learning
21.	Zeros and Poles	1	CLO2, CLO4	Video Lecture , PPT <u>https://www.youtu</u> <u>be.com/watch?v=U</u> <u>hZ5UjR5NPE</u>	Group discussion	Experiential Learning
22.	The local mapping	2	CLO2, CLO3, CLO4,	Lecture, Chalk and talk	Presentation, Group reading and discussion.	Problem-based Learning
23.	The Maximum Principle - chains and cycles.	2	CLO2, CLO3, CLO4,	Lecture, Chalk and talk	Presentation, Group reading and discussion.	Problem-based Learning
		1		UNIT-III	[	
24.	The Calculus of Residues: The Residue theorem	3	CLO2, CLO4	Lecture, PPT	Group discussion	Experiential Learning
25.	The Argument principle	2	CLO2, CLO3	Lecture PPT	Peer teaching	Participatory Learning
26.	Evaluation of definite integrals	2	CLO3, CLO4	Lecture, Demonstration	Student seminar	Experiential Learning
27.	Harmonic functions: The Definitions and basic Properties	3	CLO1, CLO4, CLO5	Lecture, Quiz, PPT	Student seminar, One Minute presentation	Participatory Learning
28.	Mean value property	3	CLO2, CLO3	Video Lecture, PPT <u>https://www.youtu</u> <u>be.com/watch?v=o</u> <u>ASPjtmFANw</u>	Group discussion	Experiential Learning
29.	Poisson's Formula.	5	CLO3, CLO4	Lecture, Chalk and talk	Presentation, Group reading and discussion.	Problem-based Learning
ł				UNIT IV		

30.	Series and Product Developments: Weierstrass theorem	4	CLO1, CLO2, CLO3, CLO4	Video Lecture Demonstration <u>https://www.youtu</u> <u>be.com/watch?v=d</u> <u>3TCJjIH5Jo</u>	Student seminar	Experiential Learning
31.	The Taylor Series - The Laurent Series	3	CLO2, CLO3, CLO4	Research article reading, Lecture, Demonstration	Group reading and discussion, Student Seminar	Experiential Learning
32.	Partial fractions Factorization: Partial Fractions - Infinite Products	4	CLO2, CLO3, CLO4	Lecture, PPT	Flipped Class room, Discussion	Participatory Learning
33.	Canonical Products.	6	CLO2, CLO3, CLO4	Video Lecture https://www.youtu be.com/watch?v=a ybXLm5hVao	Design thinking	Problem-based Learning
				UNIT-V		
34.	The Riemann Mapping Theorem - Statement and Proof-	1	CLO2, CLO4	Video Lecture,PPT <u>https://www.youtu</u> <u>be.com/watch?v=E</u> <u>J5dfUIYdFw</u>	Group reading and discussion	Experiential Learning
35.	Boundary Behavior	1	CLO2, CLO4	Lecture, Discussion, Spotter's	Group discussion, Hand's on	Experiential Learning
36.	Use of the reflection principle	3	CLO2, CLO3	Lecture, Assignment	Flipped Class room, Discussion	Participatory Learning
37.	Analytic arcs	2	CLO3, CLO4	Lecture, Seminar	Flipped Class room, Discussion	Participatory Learning
38.	Conformal mapping of Polygons: The Behavior at an angle	5	CLO2, CLO3, CLO4	Video Lecture PPT, Socrative <u>https://www.youtub</u> <u>e.com/watch?v=DG</u> <u>QIS3jhL1w</u>	Design thinking	Problem-based Learning
39.	The Schwartz - Christoffel Formula - Mapping on a rectangle.	6	CLO2, CLO3, CLO4	Video Lecture, Assignment <u>https://www.youtu</u> <u>be.com/watch?v=V</u> <u>qpFEgKD6c8</u>	Brainstorming, Optimization and Presentation	Problem-based Learning

Name of the course	Complex Analysis
Name of the Faculty	Dr. M. NILA
Participatory Learning	30 %
Experiential Learning	30 %
Problem-based Learning	40 %

COURSE NUMBER	COURSE NAME	CATEGORY	L	Т	Р	CREDIT
MTH2310	TOPOLOGY	THEORY	88	2	-	5

- > Students will learn the fundamental concepts of point-set topology.
- > Introduce students to the concepts of open and closed sets abstractly, not necessarily only on the real line approach.
- > Provide the awareness of tools to students to carrying out advanced research work in pure mathematics

#### **Course Learning Outcomes**

Upon the successful completion of the course, students will be able to

CLO	CLO Statement	Knowledge
Number		Level
CLO1	Understand the concept of topological spaces and continuous functions, concept of product topology and quotient topology	K2
CLO2	Apply the concepts of distance between two sets, connectedness, denseness, compactness and separation axioms.	К3
CLO3	Analyze the concepts to read and write theorem proofs in topology	K4
CLO4 S	Evaluate that a given point in a topological space is either a limit point of not for a given subset of a topological space.	К5
CLOStrong; I	<b>VENdetdithmone-thopy</b> oofs to do variety of examples and counter examples in topology	К5

CLOs\PLO	PLO1	PLO2	PLO3	PLO4	PLO5	Μ
CLO1	S	S	S	М	S	L
CLO2	S	S	S	S	S	
CLO3	S	S	М	S	М	
CLO4	S	М	S	S	М	
CLO5	S	S	М	S	S	

#### Mapping with Programme Learning Outcomes

S- Strong; M-Medium; L-Low

#### **CORE X – SEMESTER III – TOPOLOGY (MTH2310)**

#### Unit I (18 Hrs) Topological Spaces - Basis for a Topology - The Order Topology - Closed Sets and Limit Points- Continuous Functions - Product Topology - Metric Topology. Unit II (17 Hrs)

Connectedness and Compactness: Connected Spaces - Connected sets in R -Components and Path Components - Local Connectedness - Compact Spaces - Limit Point Compactness -Local Compactness.

#### **Unit III** Countability and Separation Axioms: Countability Axioms - Separation Axioms -Urysohn's Lemma – Urysohn Metrization Theorem.

#### **Unit IV**

The Tychonoff Theorem - Completely Regular spaces - The Stone-Cech **Compactification.** 

Unit V

#### (19 Hrs) Complete Metric Spaces - Compactness in Metric Spaces - Point-wise and Compact Convergences – Ascoli's Theorem - Baire spaces.

#### **Text Book**

S. No	Author	Title of the book	Publishers	Year &
				Edition
1.	James R.Munkres	Topology A First Course	Prentice Hall of	2000,II
			India Pvt. Ltd, New	
			Delhi	
	Unit I : Chapter 2	2 -Sections 12 -15,17 -20		
	Unit II : Chapter 3	3 -Sections 23 -29		
	Unit III : Chapter	4 -Sections 30,31,33,34		
	Unit IV : Chapter	5 -Sections 37,38		
	Unit V : Chapter	7 -Sections 43,45,46,47,48		

# (17 Hrs)

# (17 Hrs)

#### **Reference Books**

S. No	Author	Title of the book	Publishers	Year &
				Edition
1.	George F. Simmons	Introduction to Topology	Tata Mc Graw -Hill	2004, II
		and Modern Analysis	Edition	
2.	J.Dugundji	Topology	Prentice	1966, II
			Hall of India	
3.	J.L.Kelley	General Topology	Van Nostrand,	1995, I
			Reinhold Co,New	
			York	
4.	L.Steen and	Counterexamples in	Holt -Rinehart and	1978, II
	J.Seebach	Topology	Winston, New York	

# **Course Designers**

- 1. Mrs. C.R. Parvathy, Assistant Professor
- 2. Mrs. M. Deepa, Assistant Professor

#### Course content and Lecture schedule

						MTH2310 - TOPOLOGY						
Module. No.	Торіс	No. of periods	CLOs	Content delivery methods	Student engagement	Participatory Learning / Experiential Learning / Problem based Learning						
				Unit – I								
1	Basis for a Topology	2	CLO1 CLO2 CLO3	Lecture, PPT	Word cloud/ Mind map / Think Write and Share	Participatory Learning						
2	The Order Topology	3	CLO1 CLO2 CLO3	Lecture, PPT	Flipped classroom, Presentation	Participatory Learning						
3	Closed Sets and Limit Points	4	CLO1 CLO2 CLO3	Video Lecture https://www.youtub e.com/watch?v=q66 98vWK3ts	Quiz(Quizalize)	Experiential Learning						
4	Continuous Functions	3	CLO1 CLO2 CLO3 CLO4	Video Lecture https://www.youtube.c om/watch?v=ePUvjsm YzVU	Diagrams, Sketch board	Problem Based Learning						
5	Product Topology	3	CLO1 CLO2 CLO3 CLO4	Lecture	Pro/con grid	Problem Based Learning						
6	Metric Topology	3	CLO1 CLO2 CLO3 CLO4 CLO5	Lecture, PPT	Word cloud/ Mind map / Think Write and Share	Participatory Learning						

7	Connected Spaces	2	CLO2 CLO3 CLO4	Lecture – Chalk and Talk / Group reading	Word cloud/ Mind map / Think Write and Share	Experiential Learning			
8	Connected sets in R	3	CLO1 CLO2 CLO3 CLO4	PPT / OER	One minute paper	Problem Based Learning			
9	Components and Path Components	3	CLO2 CLO3 CLO4	Video Lecture https://www.youtube.c om/watch?v=2i- 49Ymf_14	Quiz(Quizalize/Socr ative)	Experiential Learning			
10	Local Connectedness	2	CLO2 CLO3 CLO4	Video Lecture. https://www.youtube.c om/watch?v=NkMpQ w1_hW8	Optimization, and Presentation	Problem-based Learning			
11	Compact Spaces	2	CLO1 CLO2 CLO4 CLO5	OER	Flipped classroom, Presentation	Participatory Learning			
12	Limit Point Compactness	3	CLO1 CLO2 CLO3 CLO4	Spotters	Hand's on(Socrative)	Experiential Learning			
13	Local Compactness	2	CLO1 CLO2 CLO3 CLO4	Lecture – Chalk and Talk/Discussion	Quiz(Quizalize/Socr ative)	Participatory Learning			
	Unit – III								
14	Countability Axioms	4	CLO1 CLO2 CLO3 CLO4	Lecture, PPT	Quiz(Quizalize/S ocrative)	Problem Based Learning			
15	Separation Axioms	4	CLO1 CLO2 CLO3	Lecture, PPT	Flipped classroom, Presentation	Participatory Learning			

16	Urysohn's Lemma Urysohn Metrization Theorem	4 5	CLO1 CLO2 CLO4 CLO5 CLO4 CLO5	Video Lecture <u>https://www.youtube.c</u> <u>om/watch?v=JUzssGzr</u> <u>-44</u> Video Lecture <u>https://www.youtube.c</u> <u>om/watch?v=FyYmpp</u> <u>kacu0</u>	Discussion Discussion	Experiential Learning Experiential Learning
				Unit – IV		
18	The Tychonoff Theorem	5	CLO2 CLO3 CLO4	Lecture, PPT	Quiz(Quizalize/S ocrative)	Problem-based Learning
19	Completely Regular spaces	6	CLO1 CLO2 CLO3 CLO4	Lecture, PPT	Word cloud	Participatory Learning
20	The Stone-Cech Compactification	6	CLO2 CLO3 CLO4	Video Lecture https://www.youtube.c om/watch?v=k6KeIU7 QWz8	Discussion	Experiential Learning
				Unit –V		
21	Compactness in Metric Spaces	5	CLO1 CLO2 CLO3 CLO4	Lecture – Chalk and Talk / Group reading	Word cloud/ Mind map / Think Write and Share	Participatory Learning
22	Point-wise and Compact Convergences	4	CLO1 CLO3 CLO4	OER	Flipped classroom, Presentation	Problem Based Learning
23	Ascoli's Theorem	5	CLO2 CLO3 CLO4	Video Lecture <u>https://www.youtube.c</u> <u>om/watch?v=aNCJZt</u> <u>WTxs</u>	Quiz(Quizalize/Socr ative)	Participatory Learning
24	Baire spaces	5	CLO1 CLO2 CLO3 CLO4	Lecture / Seminar	Diagrams, Sketch board	Participatory Learning

Name of the course	Topology
Name of the Faculty	Dr R Sasirekha
Participatory Learning	42 %
Experiential Learning	31 %
Problem-based Learning	27 %

COURSE	COURSE NAME	CATEGORY	L	Т	Р	CREDIT
NUMBER						
MTH2311	BASICS OF CRYPTOGRAPHY	THEORY	<b>88</b>	2	-	5

- Gain cyber security skills required for senior level careers by focusing on principles and best management techniques.
- Provides a deeper understanding into cryptography, its application to network security, threats/vulnerabilities to networks and countermeasures.
- > To work for financial institutions and consultancies, and as security specialists within a wide range of companies and R&D organizations.

#### Course Learning Outcomes

Upon the successful completion of course, the students will be able to

CLO	CLO	Knowledge
No.	Statement	level
CLO1	Understand the basic concept of Cryptography and Network Security,	$K_2$
	their mathematical models.	
CLO2	Apply the mathematical foundation required for various cryptographic	<b>K</b> <sub>3</sub>
	Algorithms. Identify and classify computer and security threats	
ClO3	Aanalyze existing authentication protocols for two party	<b>K</b> 4
	Communications.	
CLO4	Evaluate the issues and structure of Authentication Service and	K5
	Electronic Mail Security, web security and IP security.	
CLO5	Create a security model to prevent, detect and recover from attacks.	$K_6$

Mapping with Programme Learning Outcomes

CLOS	PLO1	PLO2	PLO3	PLO4	PLO5
PLOS					
CLO1	S	S	S	S	S
CLO2	S	S	S	Μ	S
CLO3	М	S	S	S	S
CLO4	S	S	S	S	S
CLO5	S	S	S	S	S

S- Strong, M- Medium, L-Low

#### CORE XI – SEMESTER III - BASICS OF CRYPTOGRAPHY (MTH2311)

#### Unit I

Introduction to Information Security: Introduction, security, critical characteristics of information, **NSTISSC security model**, components of an information system, security components, Approaches to information security implementation. The system development life cycle, **The Security System Development life cycle.** The need for security: Business needs first, threats, attacks, secured software development.

Cryptography : Basic concepts of cryptography, Cryptograph tools. Authentication, Passwords, keys versus passwords, **Attacking Systems via passwords**, Password verification. **Unit II** (19 hrs)

Classical Encryption Techniques: Symmetric cipher model, substitution techniques, Transposition Techniques. Block Ciphers and the **Data Encryption Standard**: Block cipher principles, the strength of DES. Introduction to Number Theory: Prime the data encryption standard Numbers, **Fermat's and Euler's Theorem**, Testing for primality, Miller-Rabin Algorithm. Chinese Remainder Theorem, Discrete Logarithms, Algorithms. (Except Problems)

#### Unit III

Public Key Crypto Systems : Principles of public-key cryptography, **public-key cryptosystems**, Applications for public-key cryptosystems, Requirements for public-key cryptography, public, key cryptanalysis, RSA Algorithm, Description of the Algorithm, Computational Aspects, Security of RSA.

Key Management: Diffie – Hellman Key Exchange – Algorithm, Key exchange protocols, Elliptic Curve Arithmetic, **Elliptic Curve cryptography**. (Except Problems)

#### Unit IV

Digital Signatures and Authentication Protocols : Requirements, Direct Digital Signature, Arbitrated Digital Signature, Authentication Protocols, Mutual Authentication, One Way Authentication, Digital Signature Standard, **DSS Approach and Digital Signature Algorithm** (Except Problem) **Unit V** (16 hrs)

Virus: **Viruses** and Related threats, Virus Counter measure Fire Walls: **Firewalls**, Types of Firewall, Design Principles of Firewall, Trusted Systems.

#### (19 hrs)

#### (18 hrs)

(16 hrs)

#### TextBooks

S.No	Author	Title of the book	Publishers		Year & Edition			
1	Dr.Michael E.	Principles and Practices of	Course Technolog	gy	2009, IV			
	Whitman Herbers	Information Security	Cengage Learning	,				
	J.Mattord							
Unit I :	Unit I : Chapter 1 : Upto SSDLC & Chapter 2							
	Chapter 8 : Upto	Cryptographic Tools						
2	William	Cryptography and Network	Pearson	2006, I	V			
	Stallings	Security	Education					
Unit II : Chapter 2 : 2.1 – 2.3 Chapter 3 : 3.1 – 3.3 & Chapter 8 : 8.1 – 8.5								
Unit III : Chapter 9 : 9.1 – 9.2 Chapter 10 : 10.1 – 10.4								
Unit IV : Chapter 13 : 13.1 – 13.3								
Unit V	Unit V : Chapter 19 : 19.1, 19.2 Chapter 20 : 20.1, 20.2							

### ReferenceBooks

S.No	Author	Title of the book	Title of the bookPublishers	
1	Straub D.W	Information Security	Prentice Hall of India, New Delhi	2009, I
2	Pachghare V.K.	Cryptography and Information Security	PHI Learning Pvt Ltd, New Delhi	2009, I
3	Boris Ryabko, AndreyFionov	Basics of Contemporary Cryptography for IT practitioners, series on coding theory and cryptology – Vol I	World Scientific Publishing Co.Re.Ltd, Singapore	2005, I

#### CourseDesigner

- 1. Mrs. R.Panneerselvi, Assistant Professor
- 2. Mr. K.Kavitha, Assistant Professor

	MTH2311 - BASICS OF CRYPTOGRAPHY								
Module No.	Topic		Module No. Topic		Topic No. of periods Content delivery method		Content delivery method	Student engagement	Participatory Learning/ Experiential Learning/ Problem based Learning
	UNIT I								
1	Introduction to Information Security : Introduction, security	1	CLO1, CLO2, CLO3	Lecture – Chalk and Talk	Word cloud/ Mind map / Think Write and Share	Participatory Learning			
2	critical characteristics of information,	2	CLO2, CLO3	PPT / OER	One minute paper	Participatory Learning			
3	NSTISSC security model	3	CLO3, CLO4, CLO5	Video / Observation <u>https://youtu.be/zd0</u> <u>U1zNBYNk</u> <u>https://youtu.be/Br</u> <u>DETY0eyJ8</u>	Group discussion	Experiential Learning			
4	Components of an information system, security components,	2	CLO1, CLO2, CLO4, CLO5	Lecture PPT	Quiz	Participatory Learning			
5	Approaches to information security implementation.	2	CLO2, CLO3, CLO4, CLO5	Lecture – Chalk and Talk/ Group readings	Optimization, and Presentation, Brainstormin g	Problem-based Learning			
6	The system development life cycle	2	CLO3,CL O4,CLO5	Lecture – Chalk and Talk	Diagrams, Sketchboard	Participatory Learning			

7	The Security System Development life cycle. The need for security: Business needs first, threats, attacks, secured software development	3	CLO2, CLO3, CLO4, CLO5	Video /Observation <u>https://youtu.be/-</u> <u>UcjG5f_FEA</u>	Group discussion	Experiential Learning
8	Basic concepts of cryptography, Cryptograph tools. Authentication, Passwords, keys versus passwords,	2	CLO2, CLO3, CLO4, CLO5	Seminar / PPT	Flipped classroom	Participatory Learning
9	Attacking Systems via passwords, Password verification	2	CLO2, CLO3, CLO4	Video / Observation <u>https://youtu.be/6gy</u> <u>f_FSx5O4</u>	Group discussion	Experiential Learning
		•	UNI	T II		
10	Classical Encryption Techniques: Symmetric cipher model,	3	CLO1, CLO2, CLO3, CLO4, CLO5	Lecture & PPT	Think Write and Share	Experiential Learning
11	Substitution techniques, Transposition Techniques.	3	CLO2, CLO3, CLO4, CLO5	Lecture & Discussion	Flipped classroom	Participatory Learning
12	Block cipher principles.	3	CLO3, CLO4	Lecture & PPT	Quiz	Experiential Learning
13	the data encryption standard, the strength of DES	3	CLO3, CLO4, CLO5	Video Lecture <u>https://youtu.be/SaZ</u> <u>GjQBItBc</u>	Group discussion	Participatory Learning
14	Introduction to Number Theory: Prime Numbers, Testing for primality,	2	CLO2, CLO3, CLO4	Lecture & Problem solving	Optimization, and Presentation, Brainstormin g	Problem-based Learning

15	Fermat's and Euler's Theorem, Miller-Rabin Algorithm.	2 3	CLO1, CLO2, CLO3	Video Lecture <u>https://youtu.be/ Y</u> <u>1c4JViJDI</u> <u>https://youtu.be/sDr</u> <u>XeCs3ghQ</u> Lecture & PPT	Diagrams, Sketchboard	Participatory Learning			
	Chinese Remainder Theorem, Discrete Logarithms, Algorithms. (Except Problems)		CLO4, CLO5		Group discussion	Experiential Learning			
	I	1	UNI		1	1			
17	Public Key Cryptosystems : Principles of public-key cryptography, public-key cryptosystems	4	CLO1, CLO2, CLO3	Video Lecture <u>https://youtu.be/1Ne</u> <u>jm_xaPbI</u>	Optimization, and Presentation, Brainstormin g	Problem-based Learning			
18	Applications for public- key cryptosystems, Requirements for public- key cryptography, public, key cryptanalysis	3	CLO1, CLO2, CLO3, CLO4	Lecture & PPT	Diagrams, Sketchboard	Participatory Learning			
19	RSA Algorithm, Description of the Algorithm, Computational Aspects, Security of RSA.	3	CLO3, CLO4	Lecture & Discussion	Post it parade	Experiential Learning			
20	Key Management: Diffie – Hellman Key Exchange – Algorithm, Key exchange protocols,	4	CLO3, CLO4, CLO5	Lecture & PPT	Diagrams,Ske tchboard	Participatory Learning			
21	Elliptic Curve Arithmetic, Elliptic Curve cryptography. (Except Problems)	4	CLO2, CLO3, CLO4	Video Lecture <u>https://youtu.be/2R</u> <u>VLBUncHJk</u> <u>https://youtu.be/ B</u> <u>CYCNYgXm8</u>	One minute paper	Participatory Learning			
	UNIT IV								

22	Digital Signatures and Authentication Protocols : Requirements, Direct Digital Signature, Arbitrated Digital Signature,	4	CLO2, CLO3, CLO4, CLO5	Lecture & PPT	Presentation	Problem-based Learning
23	Authentication Protocols, Mutual Authentication,	4	CLO2, CLO3, CLO4	Lecture & Discussion	Optimization, and Presentation	Problem-based Learning
24	One Way Authentication,	3	CLO1, CLO2, CLO3	Lecture & Assignment	Post it parade	Experiential Learning
25	Digital Signature Standard , DSS Approach and Digital Signature Algorithm (Except Problem)	4	CLO3, CLO4, CLO5	Video Lecture <u>https://youtu.be/FO</u> <u>WYDeTNRQ4</u> <u>https://youtu.be/EY</u> <u>OmHSxSOMA</u>	Diagrams,Ske tchboard	Participatory Learning
			UNI	ΓV		1
26	Virus:Viruses and Related threats	4	CLO1, CLO2, CLO3	Video Lecture <u>https://www.courser</u> <u>a.org/lecture/aruba-</u> <u>network-security-</u> <u>basics/viruses-</u> <u>UPwsb</u>	Student seminar	Experiential Learning
27	Virus Countermeasure	3	CLO1, CLO2, CLO3, CLO4	Lecture & PPT	Optimization, and Presentation, Brainstormin g	Problem-based Learning
28	Fire Walls: Firewalls, Types of Firewall	4	CLO1, CLO2, CLO3, CLO4, CLO5	Video Lecture <u>https://youtu.be/j8X</u> <u>8kiGalYI</u>	Student seminar	Experiential Learning
29	Design Principles of Firewall, Trusted Systems.	4	CLO2, CLO4, CLO5	Lecture & Assignment	Optimization, and Presentation	Problem-based Learning

Name of the course	BASICS OF CRYPTOGRAPHY
Name of the Faculty	Dr R Anitha Cruz
Participartory Learning	40%
Experiential Learning	20%
Problem based Learning	40%

COURSE	COURSE NAME	CATEGORY	L	Т	Р	CREDIT
NUMBER						
MTH2312	FLUID DYNAMICS	THEORY	88	2	-	5

- To familiarize the students with basic concepts of Fluid Dynamics as the subject has got application in medical, astrophysical, geophysical, agricultural, aero dynamical and other related disciplines.
- To develop the problem-solving skills essential to fluid dynamics in practical applications.

#### **Course Learning Outcomes**

Upon the successful completion of the course, students will be able to

CLO Number	CLO Statement				
Tumber		8			
CLO1	Understand the fundamental knowledge of fluids and its properties	K2			
CLO2	Apply the concepts and equations of fluid dynamics	K3			
CLO3	Analyze thermodynamic control volume concepts in fluid dynamics for applications that include momentum, mass and energy balances	K4			
CLO4	Evaluate the approximate solutions of the Navier-Stokes equation	K5			
CLO5	Create a role of fluid dynamics in day-to-day life	K6			

#### Mapping with Programme Learning Outcomes

CLOs\P LOs	PLO1	PLO2	PLO3	PLO4	PLO5
CLO1	S	М	S	S	М
CLO2	S	S	S	S	М
CLO3	S	S	S	S	S
CLO4	S	S	S	S	S
CLO5	S	S	М	S	S

S- Strong; M-Medium; L-Low

#### CORE XII – SEMESTER III - FLUID DYNAMICS (MTH2312)

#### Unit-I

Introductory Notions - Velocity - Streamlines and path lines - Stream tubes and filaments- Fluid body - **Density - Pressure - Differentiation following the fluid** - Equation of continuity - Boundary condition - Kinematical and physical - Rate of change of linear momentum - Equation of motion of an inviscid fluid.

#### Unit-II

Euler's momentum theorem - **conservative forces** - Bernoulli's theorem in steady motion - **Energy equation for inviscid fluid** - Circulation - Kelvin's theorem - Vortex motion - Helmholtz equation.

#### **Unit-III**

Two dimensional motion - Two dimensional functions - **Complex potentia**l - basic singularities - Source and sink vortex - Doublet - circle theorem - flow past a circular cylinder with circulation - **Conformal transformation** - Blasius theorem - Lift force.

#### **Unit-IV**

Viscous flows - Navier-stokes equations - Vorticity and circulation in a viscous fluid -Steady flow through an arbitrary cylinder under pressure - **Steady couette flow** between cylinders in relative motion - **Steady flow between parallel planes**.

#### Unit-V

Laminar boundary layer in incompressible flow - Boundary layer concept - boundary layer equations - displacement thickness - **momentum thickness - kinetic energy thickness** - integral equation of boundary layer - flow parallel to semi-infinite flat plate - Blasius equationand its solution in series.

S. No	Author	Title of the book	Publishers	Year & Edition			
1.	L.M. Milne Thomson	Theoretical Hydro	Dover Publications,	2011, V			
	Units I & II	Dynamics	New edition				
2.	N. Curle and H.J. Davies	Modern Fluid	D.Van Nostrand	1998, I			
	Units III, IV & V	Dynamics	Company Ltd,				
		Volume I	London				
	Unit I & II : Chapter I : 1.	0 -1.3					
	Chapter III: 3.10 – 3.53 omit 3.32 - 3.44						
	Unit III-IV & V: Chapter I	II : 3.1 –3.7.5. omit 3.	.4(full) and 3.5 -3.5.3				
	Chapter V	V: 5.1–5.3.3 Ch	apter VI : 6.1 - 6.3.1. O	mit 6.2.2			

#### TextBooks

#### (18 hrs)

(17 hrs)

#### (18 hrs)

(17 hrs)

(18 hrs)

#### **Reference Books**

S. No	Author	Title of the	Publishers	Year &
		book		Edition
1	F.D Shanti Swarup	Fluid Dynamics	Krishna Prakashan media P (Ltd) Meerut	2000, XIII
2	M.D Raisinghania	Fluid Dynamics (with Hydrodynamics)	S.Chand & Company	2003, V

# **Course Designer**

- 1. Mrs.R.Panneerselvi, Assistant Professor
- 2. Mrs.S.Aiswarya, Assistant Professor

#### **Course content and Lecture schedule**

	MTH2312 - FLUID DYNAMICS						
Module No.	Topic	No. of periods	CLO level	Content delivery method	Student engagement	Participatory Learning / Experiential Learning / Problem based Learning	
				UNIT I			
1	Introductory Notions - Stream tubes and filaments	3	CLO1, CLO2, CLO4	Chalk and talk, Lecture	Quiz (Quizalize/ Socrative)	Participatory Learning	
2	Velocity - Streamlines and path lines	3	CLO2, CLO3, CLO4, CLO5	Lecture, Chalk and talk	Word cloud/ Mind map / Think Write and Share	Participatory Learning	
3	Fluid body - Density Pressure	3	CLO3, CLO4	Video Lecture https://nptel.ac.in/course s/112104118	Post it parade	Experiential Learning	
4	Differentiation following the fluid - Equation of continuity -	2	CLO2, CLO4	Video Lecture, Quiz https://nptel.ac.in/course s/112104118	Diagrams, Sketchboard	Participatory Learning	
5	Boundary condition - Kinematical and physical -	3	CLO3, CLO4, CLO5	Lecture, PPT	Diagrams, Sketchboard	Experiential Learning	
6	Rate of change of linear momentum. Equation of motion of an inviscid fluid	3	CLO3, CLO4, CLO5	Chalk and talk	Think write and share	Experiential Learning	
				UNIT II			

7	Euler's momentum theorem - conservative forces -	4	CLO1, CLO2, CLO3	Chalk and talk and video Lecture https://nptel.ac.in/cour ses/112104118/14	Think write and share	Experiential Learning
8	Bernoulli's theorem in steady motion	4	CLO2, CLO3, CLO5	Lecture and chalk and talk	Presentation	Problem-based Learning
9	Energy equation for inviscid fluid	3	CLO2, CLO4	Video Lecture, Assignment https://nptel.ac.in/course s/112104118/14	Flipped classroom, Presentation	Participatory Learning
10	Circulation Kelvin's theorem	4	CLO2, CLO3, CLO5	Lecture, Quiz	Diagrams, Sketchboard	Experiential Learning
11	Vortex motion - Helmholtz equation.	3	CLO2, CLO4	Lecture, PPT	Presentation	Problem-based Learning
				UNIT III		
12	Two dimensiona l motion - Two dimensiona l functions	4	CLO1, CLO3, CLO4	Lecture,chalk and talk	Group discussion	Experiential Learning
13	Complex potential - basic singularities - Source and sink vortex	4	CLO2, CLO3, CLO5	Video Lecture <u>http://web.mi</u> <u>t.edu/16.unified/www/</u> <u>FALL/fluids/Letures/f</u> <u>15.pdf</u>	Peer teaching	Participatory Learning
14	Doublet - circle theorem	3	CLO2, CLO4	Lecture chalk and talk	Group discussion	Experiential Learning

15	flow past a circular cylinder with circulation Conformal transformat ion - Blasius theorem -	3	CLO3, CLO4, CLO5 CLO1, CLO4, CLO5	Lecture, Assignment Video Lecture, Quiz http://web.mit.edu/16.u nified/www/FALL/fluid s/Letures/f15.pdf	Group discussion Group reading and discussion	Experiential Learning Problem-based Learning
	Lift force .					
				UNIT IV	I	1
17	Viscos flows - Navier-stokes equations - Vorticity and circulation in a viscous fluid	4	CLO1, CLO3, CLO4	Lecture, chalk and talk	Student seminar, One Minute presentation	Participatory Learning
18	Steady flow through an arbitrary cylinder under pressure -	5	CLO1, CLO2, CLO4	Lecture, PPT chalk and talk	Group reading and discussion	Problem-based Learning
19	Steady couette flow between cylindersin relative motion	5	CLO2, CLO5	Lecture, Assignment https://nptel.ac.in/cou rses/101103004/27	Flipped Class room, Discussion	Participatory Learning
20	Steady flow between parallel planes.	4	CLO1, CLO3, CLO5	Lecture, Quiz https://nptel.ac.in/courses/	Peer teaching	Participatory Learning
				UNIT V		
21	Laminar boundary layer in incompressible flow	5	CLO2, CLO3	Lecture,PPT	Group reading and discussion	Experiential Learning

22	Boundary layer concept - boundary layer equations - displacement thickness	4	CLO3, CLO5	Lecture, Assignment	Group discussion	Experiential Learning
23	momentum thickness - kinetic energy thickness - integral equation of boundary layer - flow parallel to semi infinite flat plate	4	CLO1, CLO4	Lecture, Quiz https://nptel.ac.in'cours es/Webcourses- contents/IIT- <u>KANPUR/FLUID-</u> <u>MECHANICS/ui/cours</u> es_home-9.htm	Group discussion	Experiential Learning
24	Blasius equationand its solution in series.	4	CLO2, CLO3	Lecture, chalk and talk	Hand's on	Experiential Learning

Name of the course	Fluid Dynamics
Name of the Faculty	Dr.P.M.Mahalakshmi
Participatory Learning	41 %
Experiential Learning	35 %
Problem-based Learning	24 %

#### **SEMESTER III – SPECIAL PAPER**

#### **RESEARCH METHODOLOGY (MTH23S1)**

**Total duration : 30 Hrs** 

**Objective** To motivate the students in Research Oriented Topics.

Research Methodology: An Introduction Meaning, Objectives, and Types of research, Research Process, Criteria of Good Research Interpretation and Report Writing why Interpretation? Technique of Interpretation, Precaution of Meaning of Interpretation: Interpretation, Significance of Report Writing, different steps in Writing report, Layout of the research Report, Types of Reports, Oral Presentation, Mechanics of writing a Research report, Precautions of Writing Research Reports

Text, Symbols, and Commands: Command names and arguments-Environments-Declarations -Lengths -Special characters -Fine-tuning text - Word division Document Layout and Organization: Document class - Page style - Parts of the document - Table of contents.

Displayed Text: Changing font - Centering and indenting - Lists - Generalized lists - Theoremlike declarations - Tabulator stops - Boxes - Tables - Printing literal text - Footnote and marginal notes - Comments within text. Mathematical Formulas: Mathematical environments - Main elements of math mode - Mathematical symbols Additional elements - Fine-tuning mathematics.

Post Script and PDF : LATEX and PostScript - Portable Document Format Math Extensions with AMS-LATEX: Invoking AMS-LATEX - Standard features of AMS- LATEX - Further AMS-LATEX packages - The AMS fonts

Research Ethics and Responsible Conduct in Research: Brief history and analytical basis of research ethics, responsible conduct in research (Honesty in Science: Integrity, Authorship, Conflicts of Interest, Privacy and Confidentiality, Informed Consent, Risk/BenefitAssessment), The legal regulation of research ethics in India (From UGC, MHRD and other governing agencies), Regulatory requirements relevant to international research.

#### Unit II

Unit I

Credits : 2

#### Unit III

# Unit IV

#### Unit V

#### (6 Hrs)

(6 Hrs)

# (6 Hrs)

# (5 Hrs)

# (5 Hrs)

### **Text books**

S. No	Author	Title of the book	Publishers	Year & Edition		
1.	C.R.Kothari	Research Methodology (Methods and Technique)	New Age International Pvt. Ltd.	Reprint 2010, I		
	Unit I: Chapters : 1,14					
2.	H.Kopka & P.W.Daly	A Guide to Latex	Addition Wiley, London	2003, IV		
	Unit II: Chapter 2 & 3Unit III: Chapter 4 & 5Unit IV: Chapters 10 &	12				
3.	Unit V https://www.glos.ac.uk/docs/download/Research/handbook-of-principles-and-procedures.pdf					

# **Reference Books**

S. No	Author	Title of the book	Publishers	Year & Edition
1.	S.D.Sharma	A Text Book of Scientific and Technical	Sarup& Sons, Nev	2007, I
		Communication Writing for Engineers and	Delhi	
		Professionals		
2.	George A. Gratzer	Math Into LaTeX: An	Springer-Verlag	1998, I
		Introduction to LaTeX		
		and AMS-LaTex		
3.	Stefan Kottwitz	LaTeX Beginner's Guide	Packt Publishing I	2011, I

### **Course Designer**

- 1. Dr. S.Aiswarya, Assistant Professor
- 2. Mrs. R. Meenambiga, Assistant Professor

COURSE NUMBER	COURSE NAME	CATEGORY	L	Т	Р	CREDIT
MTH23E5	MATHEMATICAL MODELLING	THEORY	58	2	-	3

- > To enable the students to learn mathematical concepts
- > To build mathematical models of real-world systems, analyze them and make predictions about behavior of these systems.

#### Course Learning Outcomes

Upon the successful completion of the course, students will be able to

CLO	CLO Statement	Knowledge
No		Level
CLO1	Understand the importance of Mathematical modeling in the real world	К2
CLO2	Apply and articulate what type of modeling techniques are appropriate for a given physical system	K3
CLO3	Analyses a mathematical model of a given physical system and analyze it, make predictions	K4
CLO4	Evaluate the findings from the methods applied for the problem	K5
CLO5	Create a analyze and simulate mathematical models	K6

#### **Mapping with Programme Learning Outcomes**

CLOs/PLOs	PLO1	PLO2	PLO3	PLO4	PLO5
CLO1	S	S	S	S	М
CLO2	S	S	S	М	S
CLO3	S	М	S	S	S
CLO4	S	S	М	S	S
CLO5	S	S	S	S	М

#### S- Strong; M-Medium; L-Low

## **ELECTIVE III – SEMESTER III - MATHEMATICAL MODELLING (MTH23E5)**

#### Unit-

**Unit-II** 

Mathematical Modeling through Systems of Ordinary differential Equations of the First Order : Mathematical modeling in population dynamics, \*Mathematical modeling in Arms Race, Battles and international Trade in terms of systems of ordinary differential equations\*-Mathematical modeling in dynamics through systems of ordinary differential equations of first order.

Mathematical Modeling through difference equations: The need for Mathematical modeling through difference equations - Some simple models - Basic theory of linear difference equations with

constant coefficients - Mathematical modeling through difference equations in economics and finance.

Mathematical Modeling through difference equations (contd.): Mathematical modeling through difference equation in population dynamics and genetics - Mathematical modeling through difference equations in probability theory - Miscellaneous examples of mathematical modeling through difference equations.

Mathematical modeling through Graphs: Situations that can be modeled through graphs – Mathematical models in terms of directed graphs - mathematical models in terms of signed graphs -Mathematical models in terms of weighted graphs.

Mathematical Modeling through calculus of Variations and Dynamic Programming: Optimization principles and techniques - Mathematical modeling through calculus of variations -Mathematical Modeling through dynamic programming.

TextBook

S. No	Author	Title of the book	Publishers	Year & Edition
1.	J.N. Kapoor	Mathematical Modelling	Willey Eastern Limited	Reprint 2000, I

# **Unit III**

**Unit-IV** 

# Unit-V

(11 hrs)

(12 hrs)

# (12 hrs)

# (12 hrs)

#### (11 hrs)

Unit I: Chapter 3: 3.1,3.2, 3.5 and 3.6
Unit II: Chapter 5:5.1 - 5.3
Unit III: Chapter 5: 5.4- 5.6
Unit IV: Chapter 7:7.1 to 7.4
Unit V: Chapter 9:9.1 to 9.3

#### ReferenceBooks

S. No	Author	Title of the book	Publishers	Year & Edition
1	D.J.G James and J.J Macdonald	Case studies in mathematical Modeling	Stanly Thames, Cheltenham	2003, I
2	C. Dyson, Elvery	Principles of Mathematical Modeling	Academic Press ,New York	2001, II

#### **Course Designer:**

- 1. Mrs. R. Panneerselvi, Assistant Professor
- 2. Mrs. D. Narmadha, Assistant Professor

#### **Course content and Lecture schedule**

	Торіс	No.of	CLOs	<b>Content Delivery</b>	Student	Participatory			
Μ		hours		Methods	engagement	Learning/Experienti			
od						al			
ule						Learning/Problem			
No						based Learning			
				IInit I					
1.	Mathematical	4		Lecture, Discussio	Discussion	Participatory			
	Modeling through			n		Learning			
	Systems of								
	Ordinary								
	differential		CLO1.						
	Equations of the		CLO2						
	First Order :								
	Mathematical								
	modeling in								
	population								
	dynamics								
2.	Mathematical modeling	4		Lecture, video	Presentation/	Experimental Learning			
	in Arms Race, Battles			Lecture	Quiz				
	and international Trade			https://slideplayer.					
	in terms of systems of			com/slide/355300					
	ordinary differential			<u>4/</u>					
	equations-		CLO1,						
			CLO2,	http://bionics.seas.					
			CLO3,	ucla.edu/education					
			CLO4	<u>/MAE_182A/MA</u>					
				E182A_Project_0					
				<u>9.pdi</u>					
				https://slideplaye					
				r.com/slide/3422					
				<u>456/</u>					
3		1		Lecture Discussio	Brainstormin	Problem based			
5.	Mathematical		$CLO^2$	n PPT Chalk &	σ	Learning			
	modeling in		CLO2,	Talk	5	Louining			
	dynamics		CLO3,	1 din					
	through systems								

of ordinary differential equations of first order.					
			Unit II		
4. Mathematical Modeling through difference equations: The need for Mathematical modeling through difference equations	3	CLO1, CLO2, CLO3, CLO4	Lecture,Discussio n, video Lecture https://youtu.be/ 4 KMohr9iCU https://youtu.be/8q GYdGLbwpc https://www- users.york.ac.uk/~ pjh503/mathemati cal_model/math_ model10.pdf	Flipped Classroom,P resentation	Participatory Learning
5. Some simple models	3	CLO2, CLO3, CLO4	PPT, https://onlinecours es.nptel.ac.in/noc2 2_ma20/preview https://towardsdat ascience.com/gans -vs-odes-the-end- of-mathematical- modeling- ec158f04acb9		Experimental Learning
6. Basic theory of linear difference equations with constant coefficients	2	CLO2, CLO3, CLO4	Lecture, PPT	Optimization and Presentation	Problem based Learning
7. Mathematical modeling through difference equations in economics and finance	3	CLO2, CLO3, CLO4	Lecture,Discussio n, video Lecture https://youtu.be/v2 Pvki35H0U	Quiz,One minute paper	Participatory Learning

				https://youtu.be/V						
				<u>zlBEcs1fj4</u>						
				Unit III						
8.	Mathematical Modeling through difference equations (contd.): Mathematical modeling through difference equation in population dynamics and genetics	4	CLO2, CLO3, CLO4, CLO5	Lecture,PPT,video Lecture https://www.slides hare.net/arupparia/ introduction-to- mathematical- modelling- 42588379 https://www.cours era.org/lecture/ord inary-differential- equations/4-2- population- dynamics-i- LNhA1	Hands on (Socrative)	Experimental Learning				
9.	Mathematical modeling through difference equations in probability theory	4	CLO1, CLO2, CLO3, CLO4	Lecture,Discussio n,	Optimization and Presentation	Problem based Learning				
10	Miscellaneous examples of mathematical modeling through difference equations.	4	CLO1, CLO2, CLO3, CLO4, CLO5	Lecture,Discussio n, video Lecture https://web.ma.ute xas.edu/users/m40 8s/m408d/Current Web/LM9-1- 2.php https://math.libret exts.org/Bookshel ves/Calculus/Map %3A_Calculus Early_Transcende ntals_(Stewart)/09 %3A_Differential Equations/9.01%	Discussion and Hands on (Socrative)	Experimental Learning				

			3A Modeling wit					
			h Differential Eq					
			uations					
Unit IV								
11	3	CL O1	Lecture, Discussio	Pro/con grid,	Participatory			
Mathematical		CLOI,	n,	Quiz	Learning			
modeling throug	;h	CLO2,		_				
Graphs: Situation	ıs	CLO3,	Quiz					
that can b	be	CLO4,						
modeled throug	;h	CL05						
graphs								
12Mathematical mod	els in 2	CLO2,	Lecture,PPT	Hands on	Experimental Learning			
terms of directed g	aphs	CLO3,		(Socrative)				
		CLO4						
13Mathematical mod	els in /		Lecture Discussio	Ontimization	Problem based			
terms of signed gra	phs -	CLO1,	n video Lecture	Optimization	Learning			
	1	CLO2,	https://youtu.be/CI	, Brainstormin	Learning			
		CLO3,	$\frac{\text{mtps.//youtu.oc/c1}}{\text{wfCxk75Wk}}$	g				
		CLO4,	WICARES WK	8				
		CLO5						
14	2		Lastura video	Word	Douticinatours			
Mathematical	3	CL O1	Lecture, video	word	Farticipatory			
models in terms		CLOI,	Lecture		Learning			
of weighted		CLO2,	<u>nups://study.com/</u>	шар				
graphs.		CLOS,	academy/lesson/gr					
		CL04,	apris-m-discrete-					
		CLOS	main-definition-					
			types-uses.ntm					
			Unit V					
15	4		Lecture, Discussio	One minute	Participatory			
Mathematical			n, video Lecture	paper, Quiz	Learning			
Modeling throu	ıgh		https://youtu.be/o-		Č			
calculus	of	CLO2,	fPT0HyF2U					
Variations a	and	CLO3,						
Dynamic		CLO4	https://youtu.be/5d					
Programming	:		RGRueKU3M					
Optimization								
principles a	and							
techniques								

16 Mathematical modeling	3	CLO2,	Lecture,PPT,Synt	Hands on	Experimential Learning
through calculus of		CLO3,	hetic	(Socrative)	
variations		CLO4			
17 Mathematical Modeling through dynamic programming.	4	CLO3, CLO4, CLO5	Lecture,Discussio n, video Lecture https://youtu.be/d ND9IsjL1lo https://www.cours era.org/lecture/ope rations-research-	Brainstormin g	Problem based Learning
			algorithms/5-6- mathematical-		
			modeling-2-0ruoh		
	1	1			

Name of the Course	MATHEMATICAL MODELLING
Name of the Faculty	Dr.T.Brindha
Participatory Learning	33%
Experiential Learning	36%
Problem based Learning	31%

COURSE NUMBER	COURSE NAME	CATEGORY	L	Т	Р	CREDIT
MTH23E6	TENSOR ANALYSIS	THEORY	58	2	-	3

- To introduce students to the fundamentals of tensor algebra.
- To expose students to mathematical applications of tensor algebra which helps them to solve diverse problems which occur in real life situations

#### **Course Learning Outcomes**

Upon the successful completion of the course, students will be able to

CLO	CLO	Knowledge
Number	Statement	Level
CLO1	Understand the concept of tensor variables and difference from scalar or vector variables.	K2
CLO2	Apply the base vectors, metric tensors and strain tensors in an arbitrary Coordinate system.	К3
CLO3	Analyze the Christoffel symbols which provide a concrete representation of the connection of (pseudo) Riemannian geometry in terms of coordinates on the Manifold.	K4
CLO4	Evaluate the Riemannan- Christoffel tensor to problems of differential geometry, Electro dynamics and relativity.	K5
CLO5	Create a tensor representation from interdisciplinary areas.	K6

Mapping with Programme Learning Outcomes

CLOs	PLO1	PLO2	PLO3	PLO4	PLO5
CLO1	S	S	S	S	S
CLO2	S	S	S	S	S
CLO3	S	S	М	S	М
CLO4	S	М	S	S	М
CLO5	S	S	М	М	S

S- Strong; M-Medium; L-Low

### ELECTIVE - III- SEMESTER III – TENSOR ANALYSIS (MTH23E6)

#### Unit I

Tensor theory: Scope of Tensor Analysis – transformation of coordinates - properties of admissible transformations of coordinates- transformation by invariance- transformation by covariance and contra variance – contra variant tensor –**covariant tensor**- tensor character of covariant and contra variant laws – algebra of tensors.

#### Unit II

**Quotient law** – symmetric and skew-symmetric tensors – relative tensors – **the metric tensor**- the fundamental and associated tensors.

#### Unit III

Christoffel's symbols – transformation of Christoffel's symbols – covariant differentiation of tensors – Ricci's theorem.

#### Unit IV

Riemann – Christoffel tensor – properties of **Riemann-Christoffel tensors** –Ricci tensor – Bianchi identitites –Einstein tensor.

#### Unit V

Riemannian and Euclidean spaces – existence theorem – the E-Systems and the generalized Kronecker deltas – application of the E-Systems to determinants – tensor **character of generalized Kronecker deltas** 

#### Text Book

S. No	Author	Title of the book	Publishers	Year & Edition				
1.	I.S.Sokolnikoff	Tensor Analysis	John Wiley	1952, II				
		Theory and Applications	and sons					
	Unit I Chapter – 2 Sections: 18 -25							
	Unit II Chapter – 2 Sections: 26 - 30							
	Unit III Chapter $-2$ Sections: $31 - 35$							
	Unit IV Chapter	r –2 Sections: 36 – 38						
	Unit V Chapter	- 2 Sections: 39 - 41						

#### (12 Hrs)

## (12 Hrs)

(12 Hrs)

(11 Hrs)

#### (11 Hrs)

#### **Reference Books**

S. No	Author	Title of the book	Publishers	Year & Edition
1.	A.W.Joshi	Matrices and tensors in Physics	New age international private limited	2003, IV
2.	A.I.Borisenko and I.E.Tarapov	Vector and tensor analysis with applications	Dover publication, New York	1968, III
3.	Pavel Grinfled	An introduction to tensor analysis and the calculus of moving surfaces	Springer, New York	2013, III

#### **Course Designer:**

- 1. Mrs. R. Panneerselvi, Assistant Professor
- 2. Mrs. D. Narmadha, Assistant Professor

			MTH23	E6 - Tensor Analysis									
Module No.	Topic	CLO level	No. of periods	Content delivery method	Student engagement	Participatory Learning / Experiential Learning / Problem based Learning							
				Unit – I									
1	Tensor theory: Scope of Tensor Analysis – transformation of coordinates - properties of admissible transformations of coordinates- transformation by	CLO1, CLO2, CLO3, CLO5	4	Lecture, Problem solving	Quiz (Quizalize/ Socrative)	Participatory Learning Participatory							
2	invariance- transformation by covariance and contravariance	CLO3	4	Lecture, Assignment	map / Think Write and Share	Learning							
3	contravariant tensor –covariant tensor- tensor character of covariant and contravariant laws – algebra of tensors	CLO1, CLO2, CLO3	3	Video Lecture <u>https://youtu.be/JgaksK</u> <u>QOIsQ</u> <u>https://youtu.be/JgaksKQ</u> <u>OIsQ</u>	Post it parade	Experiential Learning							
4	algebra of tensors	CLO2, CLO3, CLO4	1	Lecture, PPT	Diagrams, Sketchboard	Participatory Learning							
				Unit – II	Unit – II								

5 6 7	Quotient law – symmetric and skew-symmetric tensors relative tensors the metric tensor-	CLO1, CLO2, CLO4 CLO2, CLO3, CLO4 CLO3, CLO5	3 3 3	Video Lecture <u>https://youtu.be/15IOIXg</u> <u>FkPE</u> Lecture, Discussion Video Lecture <u>https://youtu.be/Dn0ZZ</u> <u>RVuJcU</u>	Think write and share Presentation Flipped classroom, Presentation	Experiential Learning Problem-based Learning Participatory Learning	
8	the fundamental and associated tensors	CLO2, ClO3, CLO4	3	Lecture &PPT	Group discussion	Experiential Learning	
Unit – III							
9	Christoffel's symbols – transformation of Christoffel's symbols	CLO1, CLO2, CLO4	4	Video Lecture <u>https://youtu.be/aZFrba</u> <u>hsyUQ</u>	Group discussion	Experiential Learning	
10	covariant differentiation of tensors	CLO2, CLO3, CLO4	4	Lecture &PPT	Peer teaching	Participatory Learning	
11	Ricci's theorem	CLO3, CLO5	4	Lecture, Assignment	Group discussion	Experiential Learning	
				Unit – IV			
12	Riemann – Christoffel tensor to Inner Product Spaces	CLO1, CLO2, CLO4	4	Lecture, PPT	Student seminar, One Minute presentation	Participatory Learning	
13	properties of Riemann- Christoffel tensors –Ricci tensor	CLO2, CLO3	4	Video Lecture <u>https://youtu.be/MkxG</u> <u>FNtLiS0</u> <u>https://youtu.be/ZhDNi</u> <u>jOEw0Y</u>	Group reading and discussion	Problem-based Learning	

14	Bianchi identitites	CLO1,	3	Lecture, Quiz	Flipped Class	Participatory		
	-Einstein tensor	CLO2,			room, Discussion	Learning		
		CLO4						
	Unit –V							
15	Riemannian and	CLO1,	3	Lecture, PPT	Group reading and	Experiential		
	Euclidean spaces	CLO2,			discussion	Learning		
		CLO3,						
		CLO4,						
		CLO5						
16	existence theorem	CLO3, CLO5	2	Lecture, Assignment	Group discussion	Experiential		
						Learning		
17	the e-systems and	CLO1,	3	Lecture, PPT	Group discussion	Experiential		
	the generalized	CLO2,				Learning		
	Kroneckerdelats –	CLO4						
	application of the							
	e-systems to							
	determinants							
18	tensor character	CLO2,	3	Video Lecture	Hand's on	Experiential		
	of generalized	CLO3,		https://www.he/OILI		Learning		
	Kronecker deltas	CLO4,		<u>nups://youtu.be/0HuZJ</u>				
		CLO5						

Name of the course	Tensor Analysis
Name of the Faculty	Dr. K. Krishnaveni
Participatory Learning	47 %
Experiential Learning	33 %
Problem-based Learning	20 %

#### **QUESTION PAPER PATTERN (PG)**

#### **CA Pattern**

Section A – 3 x 2 = 6 Section B – 3 x 5 = 15 (either or – same CLO Level) Section C – 3 x 8 = 24 (either or – same CLO Level) Total 45

#### **ESE Pattern**

Section A – 5 x 2 = 10 Section B – 5 x 5 = 25 (either or – same CLO Level) Section C – 5 x 8 = 40(either or – same CLO Level) Total 75 I Year PG

CIA Test	-	5	Conducted for 45 marks after 50 days
Model Exam	-	7	Conducted for 75 marks
(Q.P. Pattern (2,5,8)	) Each	Unit 15	Marks)
Sem/Ass/Quiz	-	5	
<b>Class Participation</b>	-	5	
Attendance	-	3	
25 + ESE	75 Mar	`ks	